Geometrical Interruption in the Nerve Anatomical Model of the Foot to Simulate Small Fiber Neuropathy

M. Z. Ul Haque1,2*, Peng Du2 and Leo K. Cheng2

1Department of Biomedical Engineering, Barrett Hodgson University, Karachi, Pakistan; muhammad.zeeshan@bhu.edu.pk
2Auckland Bioengineering Institute, University of Auckland, Auckland, New Zealand;

Abstract

Diabetic Foot Ulceration (DFU) is a type of Small Fiber Neuropathy (SFN) which usually arises in the unmyelinated smaller Intra-Epidermal Nerve Fibers (IENF) of the foot. Skin biopsy is a diagnostic method to examine quantitatively IENF in the foot but examination is limited to the specific positions of the body. Computational models may provide an alternative approach to examine SFN. Formerly, an anatomical model of Normal IENF (NIENF), based on IENF Density (IENFD) at various locations in the human foot was presented. Therefore, in this study, a geometrically Interrupted IENF (IIENF) model is developed using reduced IENFD, to simulate SFN at miscellaneous locations of the human foot. This IIENF model was then compared with the NIENF model for the same location of the foot and observed reduced IENF network in this IIENF model as compared to NIENF model. Furthermore, approximately 98% of the realistic IENF terminals at the skin were generated using the modified Monte Carlo Algorithm (MCA) and the reduced empirical IENFD at the various locations of the foot. This IIENF model provides a starting platform for evaluating diabetic foot ulceration. The IIENF model may be used in future studies for functional consequences by stimulating the most distal sensory IENF of the skin of the foot.

Keywords: Diabetic Foot Ulceration, Computational Model, Intra-Epidermal Nerve Fiber, Monte Carlo Algorithm, Skin Biopsy, Small Fiber Neuropathy

1. Introduction

A major organ in the human body is the skin and its main function includes sensory perception, thermoregulation, and host defense. Epidermis and dermis are the two larger layers of the skin. The human skin comprises not only of encapsulated neural receptor but also consists of non-encapsulated free nerve terminals, called Intra-Epidermal Nerve Fibers (IENF) and they are present at the peripheral side of the sensory nerves. IENF lose their myelin sheath as they traverse the dermal-epidermal intersection of the skin and are usually unmyelinated axons. The IENF Density (IENFD) is an important quantitative measure to calculate the number of positive nerve fibers transferring the dermal-epidermal intersections per mm length of the epidermal surface. The IENFD remains mostly constant throughout the life of healthy subjects. The IENFD is also likely to be determined by anatomical location and a general reduction in IENFD is often in relation to its distance from the dorsal root ganglion.

The major complication of the diabetes mellitus is Diabetic Foot Ulceration (DFU) with a life span increased risk of approximately 15-25% larger in contrast to healthy foot. Neuropathic and neuro-ischemic are the types of DFU with an occurrence rate of 50% each from diabetes patients. International working group on diabetic foot and clinical guideline of the American diabetes association provide a general guideline for the improvement and prevention of DFU and that includes patient education, routine foot inspection, daily foot examination, glucose
monitoring, lipid administration, blood pressure monitoring and curative foot wear. The healing duration of DFU depends on incorporate standard care and etiologic factors. Previous study suggested the average healing time courses of DFU was eight weeks. Therefore, elevated efforts are required for the examination of DFU by performing diagnostic studies so that the risk of DFU is minimized.

Skin biopsy is a useful tool for determining the IENFD in DFU which involve small fiber neuropathy (SFN). This method is used for the morphological assessment of a diabetic patient when the peripheral nerve is damaged. There is a decrease in IENFD, examined in diabetic neuropathy at various anatomical positions of the human foot. It is not possible to obtain the empirical histological IENFD data from the entire foot skin in normal and DFU due to complex epidermal-dermal structures as well as large anatomical area. Therefore, quantitative IENFD data offer a useful stage for the generation of synthetic IENF network on whole foot’s skin by examining the IENF structure. It is done by using the bifurcated tree generation algorithm as mostly IENF have a bifurcated tree structure.

Therefore, in this study we modified our previously developed anatomical Normal IENF (NIENF) model using the revised Monte Carlo Algorithm (MCA). The modification was done by incorporating anatomical interruptions in the IENF model and literature based reduced IENFD to simulate SFN. For this purpose, following phases were included in the construction of the anatomically IIENF model.

2.1 Common Locations for Diabetic Foot Ulceration

The following locations of the foot model were selected for the development of the synthetic IIENF model as they are the most common locations for DFU.

- The lateral location of the foot close to the lateral malleolus was selected. This location has been suggested by the European Federation of Neurological Science (EFNS) with a sensitivity and specificity of approximately 75% for the quantification of IENFD for diagnosing length dependent peripheral neuropathy.
- The dorsal region just above the extensor brevis muscle was selected as there was a reduced IENFD observed in this exact location for a diabetic neuropathy patient.
- The medial malleolus region of the foot was chosen as this location was showed a reduced IENFD in diabetic neuropathy using skin biopsy.
- The metatarsal head region of the foot was selected since a majority of diabetic foot ulcers initially develop at this location.
- The plantar region of the great toe and the plantar heel side were also chosen since these sites were most frequently afflicted with diabetic foot ulcers.

2.2 Data Point Generation

The exterior surface of a 3D anatomical foot model developed previously by Fernandez et al. acted as an input for the construction of the synthetic IIENF model. The foot model was represented as a 2D host mesh on which regular data points were distributed, as described by Fernandez. The nerve terminals were generated through projection from the points to the exterior surfaces of the human foot model. These data points were generated with evenly spaced, regular computational points in the form of a square matrix on the exterior element of the human foot model. Here, the data points on the exterior areas were characterized with IENFD. The data points were computed from the IENFD on different areas of the foot, as deduced from anatomical study.
2.3 Anatomical IIENF Model

The modified MCA was employed for the development of anatomical IIENF model in the diverse locations of the foot\textsuperscript{23}. This algorithm depends on the center of mass theory over the surface in a defined area and is explained in detail previously\textsuperscript{23}. This algorithm was adapted due to its relative ease in generating the bifurcated tree structure for the predefined datum points and also less computationally expensive for the designated area of influence in 3D. Once the nerve terminals over the external surfaces of the different region in the foot model were generated, a bifurcated synthetic nerve tree was developed from each of the cutaneous branches in the various DFU locations. Later on, this initial bifurcated tree network was applied to develop the IENF interrupted network at different locations using modified MCA.

The synthetic anatomical IIENF model was then developed by employing revised MCA\textsuperscript{23} at the various cutaneous distributions of the human foot. It was achieved by following the various diabetic foot locations for the dorsal and plantar sides of the normal and SFN. The developed synthetic comprehensive IENF model was based on IENFD data for the normal and the SFN patients. The previously selected parameter values were used for the construction of the IIENF structural model and these parameter are branching angle limit of 60°, branch length limit of 0.01 mm, branching fraction of 0.4 and a diameter of 1.5 µm\textsuperscript{21}. These parameter values were selected in order to generate the rational number of nerve terminals in contrast to the computed number of nerve terminals and also utilized the majority of the data points of the specific region in the normal and diabetic foot\textsuperscript{21}.

3. Results

The sample interrupted computational data point's projection on the external dorsal great toe face of the foot model, based on the IENFD using cubic Hermite basis function is given in Figure 1. These data points are generated in the form of a regular grid scheme with equal space. The computational data points are evenly space in the local $\xi$-coordinate system as represented in Figure 1.

The developed anatomical IIENF model based on the IENFD for SFN was then compared with the NIENF model at the same region and their simulated results are presented in Table 2. Table 1 represents that the number of terminal branch generations, computed nerve terminals, and the produced nerve terminals are considerably reduced in this anatomical IIENF model as compared to the NIENF model in the same area of the foot with the same number of cutaneous nerve branches from the larger nerves of the foot in the normal healthy subjects.

4. Discussions

The IENFD quantitative data in the normal and SFN patients are limited for the various locations of the foot apart from plantar regions and these locations were aforementioned in section 2.1. In this study, the IENFD data for the plantar region was assumed as it was based on the fact that palmer or (non-hairy) surface of the hand is similar to the sole side of the foot\textsuperscript{34}. Consequently, the proportion of 0.548 and 0.511 was selected to compute the IENFD at the plantar side of the normal and the dia-
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betic foot as these ratios was empirical between the hairy and non-hairy skin at the human wrist surface for the normal and SFN subjects\(^{26,27}\). Similarly, the number of nerve terminals in the different position of the normal as well as SFN patient was scaled by a portion of 100 so that a whole IENF model with a realistic nerve terminals were constructed computationally and the number of computed nerve terminals in the NIENF and IIENF models are mentioned in Table 1.

Although the modified MCA was able to construct a realistic number of nerve endings in different segments of the foot, there were still some smaller limitations in using this algorithm. The main limitation was that, it did not occupy the exact locations of the generated data points. Although it generated the nerve terminals in locations nearby the data points due to the branch length limit was larger than the selected length limit and therefore, terminated at the closest data points locations. Also, the number of calculated nerve terminals was scaled by a factor of 100 in order to reduce the computational time for the generated IENF structures, although the generated nerve terminals were approximately 98% of the scaled nerve terminals. The

<table>
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<tr>
<th>Region of the foot</th>
<th>IENFD (nerve terminals/mm)</th>
<th>References</th>
<th>Number of cutaneous branches</th>
<th>Mean terminal branch generation</th>
<th>Computed number of nerve terminals</th>
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Table 1. Comparison of the IENF network between the generated normal and interrupted synthetic IENF model at the various region depend on the IENFD of normal subjects and SFN patients.
number of generated nerve terminals at some locations did not match the scaled nerve terminals.

Future research should focus on refining this algorithm so that it may be used to examine the structural changes in the IENF network by producing an accurate number of generated nerve terminals in conjunction with the computed number of nerve terminals. The generated IENF network resolution could be enhanced by decreasing the scaling to 50 or less so that it may generate more nerve terminals at the foot’s surface. This will help to create a more realistic biological IENF network that has a greater number of nerve terminals at the surface of the foot. Furthermore, future research should focus on developing the synthetic dermal plexus and various types of mechanoreceptors and these could be incorporated with the free nerve terminals so as to construct an additionally realistic anatomical nerve model in the foot’s skin.

5. Conclusions

A complete anatomical IIENF model was developed to simulate the DFU in the various locations of the human foot. The empirical reduced IENFD at different region of the foot was used in this IIENF model. The reduced number of generated nerve terminals was observed in this anatomical IIENF model as compared to the NIENF nerve model in the similar location of the foot with the same number of cutaneous nerve branches from the larger nerves of the foot. The simulation study confirmed that approximately 98% of the realistic IENF terminals at the skin of the foot were generated using the modified MCA and the empirical IENFD at the various locations of the foot. This IIENF model creates the groundwork for simulating DFU in prospective studies, where it may provide tools to clinicians and physiologists for examining structural consequences of diabetic neuropathy in its initial stages.

6. Acknowledgements

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